

## **(-1)-Reconstruction of the Decomposables**

### **Solution of $M_n$**

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#### **Abstract**

The topic of reconstructing a relationship was raised in two different ways by S. Ulam (1960) and R. Fraise (1970). If the constraints  $R/E-X$  and  $R-/E-X$  are isomorphic for each element  $X \in E$ , then  $R$  and  $R$  are also isomorphic. The first falls under the weak hypotheses of  $E$  being a set and  $R, R$  being two relations with base  $E$  and the same arithema.

If the constraints  $R/X$  and  $R/X$  are isomorphic for each stringent portion  $X$  of  $E$ , then  $R$  and  $R$  are also isomorphic, according to the second assertion.

In this study, we demonstrate that the requirement is satisfied by the decomposable tournament  $M_n$  undergoing (-1) reconstruction.

$R \succ A_1, A_2, A_3, A_4, A_5$   
and  $R \succ B_1, B_2, B_3, B_4$

**Key words:** decomposable Tournament, Reconstruction, Relation, 3-cycle, 4-cycle, Bounds, interval, isomorphic.

#### **1.Introduction**

We may represent the binary relation  $R$  as a dilation of a finite chain  $C$ . The points are therefore replaced with one of the following relations: We see that  $c$  has at least two points and differs from  $R$  whether it is a chain, 3-cycle, 4-cycle, or  $M_k$ . If  $|c|=2$ , we get two classes,  $C_1$  and  $C_2$ , and the answers are as follows:

- One of such classes is a 4-cycle, whereas the other is either a 3-cycle or a 4-cycle.
- One is  $M_k$ , and the other is random [4] and [5].

If  $|c|$  is 3, then the answers are as follows:

One class is a 4-cycle, one is a 3-cycle or 4-cycle, and the others are 3-cycle, 4-cycle, or chains. Alternatively, one type is a  $M_k$ , while the others are 3-cycle, 4-cycle, chain, or  $M_k$ .

We see that there is a decomposable solution that does not include  $M_n$  but rather all of the aforementioned solutions, at least one of which contains a 4-cycle.

**2. Tournaments characterization of  $m_n$**

The tournaments  $m_n$  are defined in such a way that  $m_n(i, j) = +$  if and only if  $i = j-1$  or  $i = j+1$ . It should be noted that  $m_4$  is a 4-cycle and  $m_3$  is a 3-cycle.

These tournaments achieved the following success:

- $m_n$  and its inverse are isomorphic.
  - $m_n$  cannot be decomposed.
  - The number of 3-cycles that pass through the vertices 1, 2, 3, ..., n is given by  $m_n$ .
- Receptivity = (1, 2, 3, 4, ... 3, 2, 1).

**3. The  $A_i$  bounds description [3] and [4]**

Allow the base by removing a 3-cycle from  $A = \{0, 1, 2, 3, 4\}$ , we get:

A1: by substituting a three-cycle for one of the points.

A2: by replacing two points with a chain of two items each.

A3: by substituting a three-chain for one of the points.

A4: defined by  $= A4/\{i, i+1, i+2\} (i \text{ mod } 5)$ , isomorphic to 3-chain.

A5: A positive diamond defined by  $= A5/\{0, 1, 2, 3\}$  when vertex equal to 0.

$A5/\{0, 1, 2, 3\}$  can be a negative diamond when vertex 1, and  $A5(2, 4) = +$ , the diamonds are formed by removing a 3-cycle one and only one of the chain's two points to form two components, 1, 2. (negative when it is equal to 2 and positive when the vertex is equal to 1)

**Notice:**

The  $A_i$  is also not deleted from the chain, as shown by B1 by the 4-chain, B1 and B2 by the 4-cycle, B3 by the positive diamond, and B4 by the negative diamond.

**4. Theorem:** R is solution of the problem  $R \not\geq A_1, A_2, A_3, A_4, A_5$  and  $R > B_1, B_2, B_3, B_4$ .

**Proof:**

1-  $R > B_1, B_2, B_3, B_4$ , obviously if one of the classes is  $M_k$ . If none of the classes are  $M_k$ . In all circumstances, there are two classes, one of which embeds a 4-cycle and the other a 3-cycle, and we can prove that  $\forall A : B_i < R$ .

2. We have  $R \not\geq A_1, \dots, A_n$  assumed that  $A_i < R$ .

-Either  $A_i$  has only one point in each  $C_i$ , or  $A_i$  is a chain (which is impossible).

-or,  $A_i$  has at least two points, and at least one of  $C_i$  is not totally contained; in this case,  $A_i$  is a chain dilate (impossible). (Based on  $A_i$ 's description)

**Corollary:**

R is the system solution, and  $R \not> B_1, B_2, B_3, B_4$  and  $R > B_1, B_2, B_3, B_4$  (-1). We know that the relation R is a dilatation of a chain C, and that each point of C may be replaced by a relation of base  $C_i$ , which is either a chain.

- A 3-cycle or a 4-cycle.
- A 4-cycle engine.
- One of the  $M_k$ .

According to Harary and Palmer's theorem, if the chain C has at least two points, R is not strong. [1]. It is known that any tournament with a cardinal greater than 4 is (1) constructible [2]. Then, if R is decomposable and has a cardinal greater than 4, R is (-1)-reconstructive. We will express the isomorphism, f between and R i, which means we must establish  $A = i=C i$ -. We write  $\forall A = C_i=C_i^-$  the R decomposition is not unique, so we start with the provided decomposition and use the following approach to get the interval I of C. When a chain 1 cardinal of known 1 delates each point of i, these chains are classified as a single type. These maximum intervals are grouped so that each class  $C_i$  is either a 3-cycle, 4-cycle, or  $M_n$ ; or a chain, in which case  $C_{i-1}$  and  $C_{i+1}$  (if they exist) are not chains. In order to investigate the isomorphism from R to  $R^-$ , we consider R and  $R^-$  to be dilatations of a chain C, with the points of C replaced by the classes  $C_i$  for R and  $C_i^-$  for  $R^-$ .

**4.1 The first proposition**

Every restriction of R of the kinds 3-cycle, 4-cycle, and  $M_n$  is entirely contained in one class of R, and the same is true for  $R^-$ .

**Proof:**

First, to prove that any 3-cycle belongs to one of the R classes it must done as follows:

If we have  $a, b \in C_i$ , and  $c \in C_j$ , with  $j \neq A$ , then we get  $R(c, a) \neq R(c, b)$ , and it follows that  $R/C_i$  is not an interval.

If i, j or k are distinct  $S_i$  two a two such as  $a \in C_i, b \in C_j, c \in C_k$ , then  $C_i, C_j$ , and  $C_k$  are the three points of C's delate.

If there is a 3-cycle in C and C is not a chain, then each 3-cycle in R is entirely contained in the class  $C_i$ , and vice versa for R. Since the final two relations may be reconverted by the sequence  $\Gamma_1, \Gamma_2 \dots \Gamma_p$  each 3-cycle is totally contained in one class. p in such a way that  $\Gamma_i \cap \Gamma_{i+1} \neq \emptyset, \forall A$ .

**Corollary:**

If  $R/C_i-x$  is a 3-cycle, 4-cycle, or  $M_n$  for all x and A, then  $f_x(C_i - x)$  is completely contained in R's class  $C_j^-$  of  $R^-$ .

**Proof:**

According to the above proposition 1, the image of a 3-cycle is a 3-cycle. which chains include a 3-cycle in the class  $C_j^-$ , a 4-cycle, and  $M_n$ . When  $R(x, y) = +$ , we say that x domains y.

When each element of  $A$  dominates in  $R$  each element of  $B$ , the part  $A$  dominates the part  $B$ . When the portion  $A$  is dominant in  $R$ , it is complementary; when it is demonized in  $R$ , it is complementary.

**Remark:** If part  $A$  is dominant in  $R$ , there is no part  $B$  dominant in  $R$  with the same cardinal as part  $A$ . Specifically, when each element of  $E-A$  dominates or is dominated by  $A$ , the subset  $A$  of  $E$  is an interval of  $R$ .

**4.2 The second proposition**

For any  $j > i$   $C_i$  and  $C_j^-$  are disjoint if the class  $R/C_i$  is a chain.

**Proof:**

If an element  $x$  exists in a  $C_i$  and a class  $C_j^-$  for  $j > i$  then there exists  $u \in C_k$  with  $k > i$  such that  $fx(u)$  belongs to the class  $C_h^-$  with  $h_i$ .

Assume that initial  $k = I + 1$ . The  $R/C_i$  class transforms into a chain, and the  $R/C_{i+1}$  class is reconverted by a 3-cycle, let  $A$ , which passes through  $u$  by the image of this 3-cycle  $A$ .

We have a contradiction when  $fx$  is included in  $C_h^-$ .

In reality, because  $u \in C_k$  and  $k > A$  for every  $y \in C_m$ , with  $m \geq i$  we obtain  $R(y, u) = +$ , which means that  $fx(y)$  belong to one class  $C_n^-$  with  $n_i$ . Let  $B$  (or  $B^-$ ) be the case. The image of  $A \cup B^-$  by  $fx$  must be included in the  $B^-$  (resp.  $B^-$ ) contradiction for the union of these classes of  $R$  (resp.  $R^-$ ) of index  $i$ . Then  $k > I + 1$ . Because all the  $C_{i+1}$  dominating points result in a conflict on the cardinal of  $B^-$  in this situation, the picture of  $C_{i+1}$  must include  $B^-$ .

**4.3 The Third proposition**

$C_i^- = C_i$  if class  $R/C_i$  is a chain.

**Proof:**

The fact that each member  $x$  of  $C_i$  belongs to the class  $C_j^-$  with  $j \leq i$  is shown above. There is no chain in the class  $R^-/C_j^-$ . In actuality, if we leave  $x$ , we won't disrupt any  $R$  by (-1)-hypo morphine cycles. Any cycle of  $R^-$  is unbreakable. The class  $C_j^-$  does not then include any cycles that pass via  $x$ .  $R^-/C_j^-$  is not a chain then. For the class  $C_j^- = I \leq j$ , we have  $i=j$ ,  $C_j^- = I \leq j$  (proposition above).

**4.4 The fourth proposition**

If the relationship  $S$  is a 3-cycle, 4-cycle, or  $M_n$  type. Consequently,  $S$  lacks an interval, where cardinal is equal to  $card(S)-1$ . The opposite, which is also a singleton, is an interval.

For example, the point that completely dominates the other or is dominated from the other, which implies that there is no such link.

**4.5 The fifth proposition of  $C_1=C_1^-$**

**Proof:**

The conclusion of the corollary above shows that the first case  $R/C_1$  is a chain. Whereas, the secondly case  $R/C_1$  is not a chain.

In the  $R/C_1$  is a 3-cycle, 4-cycle, or  $M_n$  in this situation. Let  $x \in C_1$  Consider the limitation of  $R$  to  $C_1-x$  and  $R^-$  to  $C_1^- -x$  if  $x \notin C_1^-$ . Via deleting  $x$ , we turn back at least three cycles in  $C_1$  that go by  $x$ , but we still have  $C_1^- -x = C_1^- \cdot C_1-x$ . When  $C_1-x$ 's image by  $fx$  becomes an interval dominant  $R^-/E-x$ , it becomes an interval dominant  $R^-/E-x$  as well. Due to the fact that  $C_1^-$  is an interval dominant  $R^-/E-x$ ,  $fx(C_1-x)$  will contain in  $C_1^-$  then rigorously contain in  $C_1^-$  and finally  $fx(C_1-x)$  will arrive an interval dominant  $R^-/C_1^-$  of cardinal equal card  $(C_1^- - 1)$  contradiction with statement (4).

**4.6 The sixth proposition  $\forall i : C_i = C_i^-$**

**Proof:**

Using induction, we demonstrate that for  $i = 1$ , assuming that is true for all  $j < i$  we place  $C = C_1 \cup C_2 \cup \dots \cup C_{i-1}$  and  $C^- = C_1^- \cup C_2^- \cup \dots \cup C_{i-1}^-$

Next, we have  $C = C^-$  if  $R/C_i$  is a chain, then it follows from corollary 3 that it is also true if it is not a 3-cycle, 4-cycle, or  $M_n$ .  $C \cup C_{i-x}$  is an interval dominating.

When  $R/E-x$  is dominant, its image by  $fx$  is an interval of  $R/E-x$ . When  $R/E-x$  is dominant, its image by  $fx$  is an interval of  $R^-/E-x$  the interval dominant  $\frac{R^-}{C^- \cup C_1^- - x}$

Because  $R/E-x$  of Cardinal is likewise an interval dominant of  $C^- \cup C_1^- - x$ , which is at least equal to Cardinal  $C \cup C_i - x$  If  $x \notin C_1^-$ .

If  $x = C_1$ , then  $fx(C) = C$ , and  $fx(C_i - x)$  is strictly contained in  $C_1^- \cdot R^-/C_1^-$ .

$C_i^- - 1$  possesses an interval of cardinal equal to card  $C_i^-$ , which is inconsistent with the proposition (4)

$R$  and  $R^-$  are isomorphic if  $R$  owns the relations  $A_1, A_2, A_3, A_4$ , and  $A_5$  as borns,  $R$  and  $R^-$  are (-1) hypomorphes, and  $R$  and  $R^-$  are two relations of the same finite base  $E$  of cardinal  $>5$ .

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